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 $\hfill \cap$ $\stackrel{\frown}{\hookrightarrow}$ rcuit Analysis and Design - Lesson 3 Lesson Plan (introduction...) Introduction Boolean laws and theorems Sum of product method Design example Handout No. 2 Worksheet No. 3 First Evaluation Karnaugh Mapping - Lesson 4 Lesson Plan (introduction...) Introduction Karnaugh map Truth table to Karnaugh map Pairs, Quads, and Octets Overlapping and Rolling Worksheet No. 4 Karnaugh Mapping II - Lesson 5 Lesson Plan (introduction...) Introduction





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Lehr- und Lernmittel, Informationen, Beratung

Educational Aids Literature, Consulting

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GTZ

Deutsche Gesellschaft fr Technische Zusammenarbeit (GTZ) GmbH

Andreas Lange

Digital Teaching Aid

91-34-0308/2



Figure

Andreas Lange, DED, 1994 Philippines





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	ASCII code
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	Gray code
	Encoder
	Decoder
	Code converter
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Coding - Lesson 6

Lesson Plan

Titel: Coding

Objectives:

- Get an idea about the purpose of codes
- Understand the principle of decoder, encoder, and code converter
- Able to design logic circuits for code conversion

Time	Method 1	Торіс	Way	Remark
		* Review Lesson 5		
		* Introduction		
		* ASCII code		
		- Coding scheme		
		- Parity bit		
		* BCD code		
		* Excess-3 code		
		* Gray code		
		* Encoder		
		- Decimal to BCD encoder		
		* Decoder		
		- BCD to decimal decoder		
		* Code converter		

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		- BCD to Exces-3 code converter		
		* Review Exercise		Worksheet No. 6
	S: Speech D: Discussion Q/A: Question/Answer F: Exercise		B: Boardscript P: Picture Ex: Example HO: Hands-On WS: Worksheet HT: Hand-Out	

Introduction

Coding

Ex: Coding \rightarrow Alphanumeric information in and out of a computer.

ASCII code

ASCII Code (American Standard Code for Information Interchange)

ASCII code is a 7 bit code whose format is

X6 X5 X4 X3 X2 X1 X0

i.e. the letter A is coded as:

$1 \ 0 \ 0 \ 0 \ 0 \ 1$

Coding scheme:

	X6 X5 X4										
Х3	X2	X1	X0	010	011	100	101	110	111		
0	0	0	0		0		Ρ		Ρ		
0	0	0	1		1	Α	Q	а	q		
0	0	1	0		2	В	R	b	r		
•	•	•	•		•	-	-	•	•		
•	•	•	•		•	•	•	•	•		
•	•	•	•		•	-	-	•	•		
1	1	1	1			0					

Ex; The letter B via ASCII in binary:

100010

Parity bit

During sending/transmitting data, 1 bit errors may occur. To catch these errors, a parity bit is usually transmitted along with the original bits:

```
X7 X6 X5 X4 X3 X2 X1 X0
```

parity bit

A parity checker at the receiving end can test for even or odd parity. I.e the transmitting station will set the parity bit always in that way to put the whole number in even parity. If the parity checker at the receiving end determines odd parity it will report an error message.

Now we have 8 bits (1 byte), this is the ideal length because most digital equipment is set up to handle bytes of data.

BCD Code (Binary Coded Decimal)

Each decimal place (0...9) is represented by a binary code.

```
Ex: 753
011101010011
7 5 3
```

The BCD code is a 4 bit code which is very common along digital systems.

Excess-3 code

Also an important 4 bit code

Ex: Convert a decimal number in excess-3 code:

 $12 \rightarrow excess-3$

1 **2** *First we add 3 to every decimal diait.* D:/cd3wddvd/NoExe/Master/dvd001/.../meister10.htm Digital Teaching Aid (DED Philippinen, 86 p.)

 $\frac{+3}{4}$ $\frac{+3}{5}$

0100 0101 *Then we convert the sum in BCD form.* 0100 0101 in excess-3 stands for decimal 12.

Fig. 6-1: Convertion table, dec \rightarrow BCD \rightarrow excess-3

Decimal	BCD	Excess - 3
0	0000	001 1
1	0001	0100
2	0010	0101
3	0011	0110
4	0100	0111
5	0101	1000
6	0110	1001
7	0111	1010
8	1000	1011
9	1001	1100

Gray code

Each Gray code number differs from the preceding number by a single bit.

Fig. 6-2: Convertion table, dec \rightarrow Gray \rightarrow BCD

Decimal	Gray	Binary
0	0000	0000
1	0001	0001
2	0011	0010
3	0010	0011
4	0110	0100
5	0111	0101
6	0101	0110
7	0100	0111
8	1100	1000
9	1101	1001

Encoder

An encoder converts an active input signal into a coded output signal.

Ex: Decimal to BCD encoder

(see Fig. 6-3 on the next page) If switch 9 is pressed:

A B C D = 1 0 0 1

The circuit in Fig. 6-3 is also available as TTL device 74147.

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Decoder

A decoder converts a coded input signal into an active output signal.

Ex; Develop a decoder circuit which converts BCD code into decimal.

Fig. 6-4: Truth table, BCD \rightarrow decimal



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	८	८ _	∠ -				
0	0	0	0	0			
0	0	0	1	1			
0	0	1	0	2			
0	0	1	1	3			
0	1	0	0	4			
0	1	0	1	5			
0	1	1	0	6			
0	1	1	1	7			
1	0	0	0	8			
1	0	0	1	9			

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To optimize the circuit we use a Karnaugh map for simplification:



Digital Teaching Aid (DED Philippinen, 86 p.) Fig. 6-5: Karnaugh map

For every number in the Karnaugh map we can write an equation:

X0=abcd
X1−ābcd
$X2 = \overline{b}c\overline{d}$
X3=bcd
X4=bcd
X5-bcd
X6-bcd
X7=bcd
X8-abcd
X9=ad

Now we can draw the logic circuit:



Code converter

Code converter are logical networks which convert codes into another.



Fig. 6-8: Convertion table, dec \rightarrow BCD \rightarrow excess-3

Dec		BC	CD)	E>	ce	ss -	• 3
	а	b	e	d	a1	b 1	C1	d 1
0	0	0	0	0	0	0	1	1
1	0	0	0	1	0	1	0	0
2	0	0	1	0	0	1	0	1
3	0	0	1	1	0	1	1	0
4	0	1	0	0	0	1	1	1
5	0	1	0	1	1	0	0	0
6	0	1	1	0	1	0	0	1
7	0	1	1	1	1	0	1	0
8	1	0	0	0	1	0	1	1
9	1	0	0	1	1	1	0	0

Worksheet No. 6

No. 1 Develop a decoder circuit for the conversion of the Gray code into the decimal system. Use a Karnaugh map to get a simplified circuit!



21/1	L0/20	11			-
	0	0	0	1	1
	0	0	1	1	2
	0	0	1	0	3
	0	1	1	0	4
	0	1	1	1	5
	0	1	0	1	6
	0	1	0	0	7
	1	1	0	0	8
	1	1	0	1	9
	X	X	X	X	
	•	•	•	•	
	•	•	•	•	

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<u>No. 2</u> Develop a code converter for the conversion of the excess 3 code into the 8421 code (BCD).

Complete the truth table!

Use Karnaugh maps to get a simplified circuit!



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1	0	1	0	0	0	0	0	1
2	0	1	0	1	0	0	1	0
3	0	1	1	0	0	0	1	1
4	0	1	1	1	0	1	0	0
5	1	0	0	0	0	1	0	1
6	1	0	0	1	0	1	1	0
7	1	0	1	0	0	1	1	1
8	1	0	1	1	1	0	0	0
9	1	1	0	0	1	0	0	1
	1	1	0	1	1	0	1	0
	1	1	1	0	1	0	1	1
	1	1	1	1	1	1	0	0
	0	0	0	0	1	1	0	1
	0	0	0	1	1	1	1	0
	0	0	1	0	1	1	1	1

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The lower six rows are redundant.



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Flip-Flops - Lesson 7

Lesson Plan

Titel: Flip-Flops

Objectives:

- Understand the Flip-Flop principle
- Know the three basic Flip-Flops (RS, D, JK)
- Able to analyze timing diagrams

Time	Method	Торіс	Way	Remark
		* Review Lesson 6		
		* Introduction		

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* RS Flip-Flops		
* Clocked RS-FF		
* Timing diagram		
* D-FF		
* FF switching time		
* JK-FF		
* JK-MS-FF		
* Review exercise		Worksheet No. 7
	B: Boardscript	
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	 * RS Flip-Flops * Clocked RS-FF * Timing diagram * D-FF * FF switching time * JK-FF * JK-MS-FF * Review exercise 	* RS Flip-Flops * Clocked RS-FF * Timing diagram * D-FF * D-FF * FF switching time * JK-FF * JK-FF * Review exercise B: Boardscript P: Picture Ex: Example HO: Hands-On WS: Worksheet HT: Hand-Out

Introduction

Flip-Flops

Sometimes there is a need of digital devices or circuits whose output will remain unchanged, once set, even if there is a change in input.

RS Flip-Flops

A Flip-Flop is a bistable electronic circuit that has two stable states.

 \Rightarrow Output is either 0 or 5V dc

The Flip-Flop can be regarded as a memory device. It can be used to store one binary digit at the output.



Fig. 7-1: RS Flip-Flop, logic circuit and device symbol

HO: What is the truth table for the circuit above?

Solution:

Fig. 7-2: Truth table, RS Flip-Flop

R	S	Q	Action
0	0	Last value	No change
0	1	1	Set
1	0	0	Reset
1	1	?	Forbidden

If both inputs (R, S) are high at once, the output can not be determined before; therefore, it is a forbidden state.

Ex: Create a RS Flip-Flop with NAND gates.



Note: The inputs (R, S) are indicated with an overbar so they are inverted.



Fig. 7-4: Logic symbol, RS Flip-Flop with inverted inputs

Clocked RS Flip-Flop



This Flip-Flop ca be enabled or disabled.

ENABLE \rightarrow low: R and S will have no effect on the output

ENABLE \rightarrow high: R and S inputs will be directly transmitted to the output

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Timing diagram

A timing diagram is a drawing to determine the time dependent actions of logic devices.



Fig. 7-7: Timing diagram of a clocked RS Flip-Flop

Fig. 7-7 shows that the inputs (R, S) effect the output (Q) only when the clock

signal (CLK) is high.

<u>RS Flip-Flop application:</u> Bounce free switch

D - Flip-Flop (D-FF)

The generation of two signals to drive a Flip-Flop is a disadvantage in many applications. This has led to the D-FF, a circuit that needs only a single data input.



Fig. 7-8: D Flip-Flop, logic circuit and truth table

 $\text{CLK} \rightarrow \text{low:}$ D can change without effect on the output

 $\mbox{CLK} \rightarrow \mbox{high:} Q \mbox{ is forced to equal the value of } D$

Ex: Create a 4 bit data memory with D-latches (D-FF).



In Fig. 7-9, when the clock goes high, input data is loaded into the Flip-Flops and appears at the output.

Suppose the data input is:

 $D_3 D_2 D_1 D_0 = 1010$

When the clock goes high this 4 bit word is loaded into the D-latches, resulting in an output of:

 $Q_3 Q_2 Q_1 Q_0 = 1010$

Flip-Flop switching time



Fig. 7-10: Timing diagram, FF switching time

- t_{set}: Minimum of time that the date bit must be present before the clock edge hits (because of stray capacitance)
- thold: The data bit has to be hold long enough for the internal transistors to switch.
- t_p: Switching time, diodes and transistors cannot switch states immediately. (some nanoseconds)

JK Flip-Flop (JK-FF)

Flip - Flops can be used to build counters, JK-FF are the ideal elements for that purpose.

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Fig. 7-11: JK-FF, logic circuit

Ex: What is the truth table for the circuit above?

Fig. 7-12: Truth table, JK-FF

CLK	J	K	Q
X	0	0	last state
	0	1	0
	1	0	1
	1	1	toggle

J and K \rightarrow Both AND gates are disabled, clock pulses have no effect. Q retains its last low: value.

 $J \rightarrow low, K$ The upper date is disabled, only reset is possible (unless O is already reset). D:/cd3wddvd/NoExe/Master/dvd001/.../meister10.htm

- - - ----

 \rightarrow high:

 $J \rightarrow high$, K The lower gate is disabled, only set is possible (unless Q is already high). $\rightarrow low$:

J and $K \rightarrow$ Set or reset is possible, the Flip-Flop will "toggle" on the next positive clock edge. Toggle means to switch to the opposite state.



Fig. 7-13: JK-FF's, logic symbols

Preset (PR) and Clear (CLR) are input signals to get a definite start point.

JK Master-Slave FF (JK-MS-FF)



Regardless what the master does, the slave copies it. The slave copies the master on the negative clock edge. This circuit provides a way to avoid racing.



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Available as TTL device: 74 LS 76

Worksheet No. 7

<u>No. 1</u> A JK master slave FF has its inputs tied to + 5V, and a series of pulses are applied to its CLK input Describe the Q output.



<u>No. 2</u> The signal drives a clocked RS - FF. If Q is low before point A in time: At what point does Q becomes a 1? What does Q reset to 0?



No. 3 Use the information in the preceding problem and draw the waveform Q.

No. 4 The signal drives a D-FF. What is the value of stored in the FF after the clock pulse is over?



<u>No. 5</u> A normal JK-FF, J = K = 1. A 1 MHz is applied to the CLK input it has a propagation delay t_p of 50 ns. Draw the input squarewave and the out put expected at Q. Be sure to show the propagation delay time.

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Second Evaluation

No. 1 In a workshop two machines are driven by an electric motor

Power consumption: motor A = 1 KWmotor B = 2 KW

For a new machine of which its motor C receives the power of 4 KW, the maximum main power of Pmax = 4 KW is sufficient only if the two other machines (A and B) are not switched on. Design a circuit which supplies a warning signal Q if a power higher than 4 KW is taken from the main power system by the three machines.

- Truth table
- Karnaugh map
- Logic circuit

No. 2 For a display of the figures 1-6, in the well known spot configuration of a game die, design the code conversion circuit. At the input the figures are binary coded.

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T, U, V, W, X, Y, Z are output variables (LED's)

- Truth table
- Karnaugh map
- Logic circuit



No. 3 Design a JK Flip Flop with NAND and AND gates.

- Logic circuit
- Truth table

No. 4 Design a D Flip Flop. Use only NAND gates.

- Logic circuit
- Truth table


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 Counter - Lesson 8

 Lesson Plan
 (introduction...)
 Introduction
 Asynchronous counter
 Synchronous counter
 Seven segment indicator and decoder
 Worksheet No. 8

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Counter - Lesson 8

Lesson Plan

Titel: Counter

Objectives:

- Understand the principle of asynchronous and synchronous counter
- Able to design asynchronous counter
- Know the seven segment principle

Time	Method	Торіс	Way	Remark
		* Review Lesson 7		
		* Introduction		
		* Asynchronous counter		
		- Timing diagram		
		- Truth table		
		- Countdown mode		
		* Synchronous counter		
		* Seven Segment Indicator and Decoder		
		- Common anode indicator		
		- Common cathode indicator		
		- Seven segment decoder		
		* Review Exercise		Worksheet No. 8
	S: Speech D: Discussion Q/A: Question/Answer F: Exercise		B: Boardscript P: Picture Ex: Example HO: Hands- On WS: Worksheet	

Introduction

Counter

Counters are beside the logic operations the basic elements of all digital controls.

Since the clock pulses occur at known intervals, the counter can be used as an instrument for measuring time and therefore period or frequency.

On principle there are two counting organisations:

- Asynchronous (serial, ripple) counter

Each Flip-Flop is triggered by the previous Flip-Flop, and thus the counter has a cumulative settling time. (Delay time, tp)

- Synchronous (parallel) counter

Here, every Flip-Flop is triggered by the clock (synchronous), and thus the settling time is simply equal to the delay time of a single Flip-Flop.

Asynchronous counter

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Fig. 8-1: Asynchronous counter with JK-MS-FF in toggle mode

To understand how this counter works lets have a look at the timing diagram:



Fig. 8-2: Timing diagram, asynchronous mod 8 counter

The frequency of waveform C is one half that at B, but is only one-eighth the clock frequency.

The FF's are negative edge triggered, hence output signals change only at the falling side of the clock pulse.

Fig. 8-3: Truth table, asynchronous mod 8 counter

CLK transition	C	B	A
0	0	0	0
1	0	0	1
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0
7	1	1	1
0	0	0	0

A three Flip-Flop counter is often referred to as a mod 8 (modulus 8) counter since it has 8 states.

 $2^3 = 8$ output conditions (*The exponent equals to the number of Flip-Flops*)

The largest decimal number which is represented by a 3 Flip-Flop counter is:

$$2^3 - 1 = 7$$

In general: 2n - 1

Count Down mode

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Switching the clock inputs of each Flip-Flop to the \overline{Q} outputs causes the counting sequence to start at 111 down to 000.

<u>HO</u>: How many Flip-Flops are required to construct a mod-128 counter? A mod-32? What is the largest decimal number that can be stored in a mod-64 counter?

Solution:

- * mod-128 must have 7 Flip-Flops (27 = 128)
- * mod-32 must have 5 Flip-Flops
- * mod-64, the largest decimal number is 63

Synchronous counter



Fig. 8-4: Synchronous counter, with JK-MS-FF in toggle mode

The negative clock transistion is the mechanism that toggles each FF. Therefore, whenever a Flip-Flop changes state, it toggles at exactly the same time as all the other Flip-Flops. In other words, all Flip-Flops change state in synchronism. This

advantage needs an increase in hardware (additional gates), hence the asynchronous counter is the cheaper solution for time uncritical applications.

Seven segment indicator and decoder

Seven segment indicators

Seven segment indicators are made by seven LED's. LED's are light emitting diodes. (LED function: Free electrons recombine with holes near the junction. As the free electrons "fall" from a higher energy level to lower one, they give up energy in form of heat and light)



Depending on which LED's are light up it is possible to indicate decimal numbers from 0 to 9.



Fig. 8-6: Seven segment indicator, common anode type

Two types of indicators are available:

- common anode
- common cathode

The diodes are controlled by ground (common anode) or by 5V (common cathode).



Fig. 8-7: Seven segment indicator, common cathode type

Seven segment decoder

Seven segment decocer are devices to drive seven segment indicators.

Ex: The 7448

(see Fig. 8-8 on the next page)



The 7448 is a decoder to drive common cathode indicators.

When the BCD input is set to:

A B C D = 0 1 0 0

The internal logic of the decoder forces the LED's b, c, f, and g to conduct.

Worksheet No. 8

<u>No. 1</u> Draw the logic diagram, truth table, and the waveform for a three flip-flop serial counter that uses JK master slave flip-flops sensitive to positive clock transition.

<u>No. 2</u> Determine the number of possible states in a counter composed of the following number of flip-flops:

a) 5 b) 8 c) 11

<u>No. 3</u> Draw the logic diagram, truth table, and waveforms for a two flip-flop serial counter operating in the count down mode.

<u>No. 4</u> Design the internal logic circuit for the 7448 (seven segment decoder for the common cathode indicator).

<u>No. 5</u> Sketch the logic circuit for the following seven segment indicators:

a) common cathode type

b) common anode type



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Data Processing Circuits - Lesson 9

Lesson Plan

Titel: Data Processing Circuits

Objectives:

- Understand the principle of multiplexer and demultiplexer
- Able to use the multiplexer solution as design method

Time	Method	Торіс	Way	Remark
		* Review Lesson 8		
		* Introduction		
		* Multiplexer		
		- Principle and logic circuit		
		-The 74 150		
		- Multiplexer design	НО	Handout No. 3
		* Demultiplexer		
		- Principle and logic circuit		
		-The 74 154		
		* Review exercise	WS	Worksheet No. 9
	S: Speech		B: Boardscript	
	D: Discussion		P: Picture	
	Q/A: Question/Answer		Ex: Example	
	E: Exercise		HO: Hands-On	
			WS: Worksheet	
			HT: Hand-Out	

Introduction

Data Processing Circuits

Data processing circuits: Logic circuits that process binary data.

Multiplexer

A multiplexer is a circuit with many inputs but only one output.





A multiplexer is also called a data selector because the output bit depends on the input data that is selected. The input bits are labeled D_0 to D_{15} . Only one of them is transmitted to the output. Which one depends on the value of A B C D, the control input.

<u>Ex:</u> If A B C D = $0 \ 0 \ 0 \ 0$

the output will be: D:/cd3wddvd/NoExe/Master/dvd001/.../meister10.htm → Y = D₀ So the input bit DO is selected. Or if A B C D = 1 1 1 1 \rightarrow Y = D₁₅

The control nibble (nibble = 4 bit) A B C D determines which of the input data bits is transmitted to the output.

The 74 150

The TTL device 74 150 is a 16 to 1 multiplexer with inverted output. (see Fig. 9-2, instead of a OR gate, a NOR gate is used to invert the output)

Ex: When A B C D = 1 0 0 1

X=D9

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Fig. 9-3: Pinout diagram, 74150 16 to 1 multiplexer

Pin 9 (STROBE) is an input signal that disables or enables the multiplexer.

Fig. 9-4: Truth table, 74 150



		_	_		
L	0	0	1	0	${\rm \overline{D}}_2$
L	0	0	1	1	${\rm \overline{D}}_3$
L	0	1	0	0	\overline{D}_4
L	0	1	0	1	${\rm \overline{D}}_{5}$
L	0	1	1	0	\overline{D}_6
L	0	1	1	1	\overline{D}_7
L	1	0	0	0	\overline{D}_{B}
L	1	0	0	1	\overline{D}_{ϑ}
L	1	0	1	0	\overline{D}_{10}
L	1	0	1	1	\overline{D}_{11}
L	1	1	0	0	\overline{D}_{12}
L	1	1	0	1	\overline{D}_{13}
L	1	1	1	0	\overline{D}_{14}
L	1	1	1	1	\overline{D}_{15}
Н	X	X	X	X	Η

With high STROBE the value of A B C D doesn't matter, the output will allways be high.

Multiplexer Logic (Multiplexer Design)

The starting point for digital design is usually the truth table. We already discussed two standard methods for implementing a truth table:

- sum of products method
- product of sums method

Now we are ready for the third method:

- the multiplexer solution

The following example explains the multiplexer solution. (Please refer to Handout No. 3)

Ex: First we have to complement each output in the truth table (Y), that will be the corresponding data input for the multiplexer:

```
Y = 1 \rightarrow 0 \rightarrow D_0

Y = 0 \rightarrow 1 \rightarrow D_1

Y = 1 \rightarrow 0 \rightarrow D_2

Y = 1 \rightarrow 0 \rightarrow D_3
```

•

and so on for every value of Y

Next, wire the data inputs of the 74 150, so that they equal the foregoing values:

•

```
\mathsf{D}_0 \to \text{grounded}
```

 $\mathsf{D}_1 \rightarrow \text{connected to } \mathsf{5V}$

 $\mathsf{D}_2 \to \text{grounded}$

 $\mathsf{D}_3 \to \text{grounded}$

 $\mathsf{D}_{15} \to \text{grounded}$

Check the circuit:

When A B C D = 0 0 0 0

 \rightarrow D₀ is the selected input since D₀ is low. Y is high

Please check also the remaining input possibilities!

Universal logic circuit

The 74 150 can be used as a design solution for any 4 variable truth table.

Demultiplexer

A demultiplexer is a circuit with only one input but many outputs.



Fig. 9-5: Demultiplexer

By applying control signals, we can steer the input signal to one of the output lines.



<u>The 74 154</u>

The 74 154 is a 1 to 16 demultiplexer, with active low STROBE and DATA input.

Fig. 9-7: Truth table, 74 154 1 to 16 demultiplexer

STROBE	DATA	A	B	C	D	Y
L	L	0	0	0	0	Y0
L	L	0	0	0	1	Y1
L	L	0	0	1	0	Y2
L	L	0	0	1	1	Y3
L	L	0	1	0	0	Y4
L	L	0	1	0	1	Y5
L	L	0	1	1	0	Y6
L	L	0	1	1	1	Y7
L	L	1	0	0	0	Y8
L	L	1	0	0	1	Y9
L	L	1	0	1	0	Y10
L	L	1	0	1	1	Y11
L	L	1	1	0	0	Y12
L	L	1	1	0	1	Y13
L	L	1	1	1	0	Y14
L	L	1	1	1	1	Y15

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L	H	XXXXH
Н	L	XXXXH
Н	Н	XXXXH

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Handout No. 3

Example for Multiplexer Solution

<u>Problem</u>: Design a logic circuit for the problem which is given through the truth table below. Use a 74150 to implement this table:



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	1	0	1	1	1					
	1	1	0	0	1					
	1	1	0	1	1					
	1	1	1	0	0					
	1	1	1	1	1					

Solution: Complement each Y output to get the corresponding data input:

D0 = 1 = 0DI = 0 =D2 = D3 = D D D D D D D



Connect: the chip in response to the list of corresponding data inputs:



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Universal Logic Circuit

This circuit is an example of multiplexer logic. You an input data pin when the corresponding output is in the truth table.

You connect an input data pin to if the corresponding output is..... in the truth table.

Worksheet No. 9

```
<u>No. 1</u> In Fig. 9-1, if
```

```
a) A B C D = 0 1 1 0
b) A B C D = 1 0 0 1
c) A B C D = 1 1 0 1
```

what does Y equal?

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Fig. 9-1: 74 150, 16 to 1 multiplexer

<u>No. 2</u> Show how to connect a 74150 (use Fig. 9-1) to implement the following Boolean equation:

 $Y = \overline{A}B\overline{C}D + A\overline{B}CD + \overline{A}BC\overline{D}$

No. 3 Draw a circuit with two 74150's that has the truth table like the following

one:

A	В	С	D	Y ₁	Y2
0	0	0	0	0	0
0	0	0	1	1	0
0	0	1	0	0	0
0	0	1	1	0	1
0	1	0	0	0	0
0	1	0	1	1	1
0	1	1	0	1	1
0	1	1	1	1	1
1	0	0	0	0	1
1	0	0	1	1	0
1	0	1	0	1	0
1	0	1	1	1	0
1	1	0	0	0	0
1	1	0	1	1	0
1	1	1	0	1	1
1	1	1	1	0	0





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Third Evaluation

<u>No. 1</u> At a distribution point of a conveyer belt a flap which is controlled by a counter circuit is to divert arriving piece-goods always six to the left and four to the right.

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The counting pulses T are supplied by a light barrier immediately before the diverting flap. The flap opens the way to the left if the control instructions are x = 1, y = 0 and to the right when x = 0, y = 1

Develop the truth table. Use the sum of product method. For the simplification use a Karnaugh map. Design the logic circuit.

Take a decimal counter with four output lines $(2^0, 2^1, 2^2, 2^3)$.

<u>No. 2</u> Sketch an asynchronous mod 16 counter. Use JK-MS flip flops.

<u>No. 3</u> Show how to connect a 74150 multiplexer (Fig. 2) to implement the following boolean equation:

 $y = \overline{A}B\overline{C}D + A\overline{B}C\overline{D} + ABC\overline{D}$

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<u>No. 4</u> Input signals R and T are low in Fig. 3. Which is the active output line when A B C D = 0011?

<u>No. 5</u> To get the y₉ output line active in Fig. 3, what are the input signals you need?





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Answers to Evaluation Problems

First evaluation:

<u>No. 1</u>



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1101	

<u>No. 3</u>



<u>No. 4</u>



 $X = AB\overline{C}D + ABC\overline{D} + ABCD$

<u>No. 5</u>

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 $X = A\overline{B} + \overline{B}D + \overline{B}C + A\overline{C}D + \overline{A}CD$

Second evaluation:

<u>No. 1</u>

A	B	C	X	
0	0	0	0	
0	0	1	0	
0	1	0	0	
0	1	1	1	Q = AB + AC
1	0	0	0	
1	0	1	1	
1	1	0	0	
1	1	1	1	

<u>No. 2</u>



5	1	0	1	1	0	1	1	1	0	1
6	1	1	0	1	1	1	0	1	1	1
7	1	1	1	x	x	x	x	x	x	X

T = Z T = B + A V = AU = Y $V = X U = AB \qquad W = C$

Second evaluation:



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Third evaluation:

<u>No. 1</u>

clock	Α	В	С	D	X	Y
0	0	0	0	0	1	0
1	0	0	0	1	1	0
2	0	0	1	0	1	0
3	0	0	1	1	1	0
4	0	1	0	0	1	0
5	0	1	0	1	1	0
6	0	1	1	0	0	1
7	0	1	1	1	0	1
8	1	0	0	0	0	1
9	1	0	0	1	0	1
	Don't care conditions					

 $X\!=\!\overline{A}\,\overline{B}\!+\!\overline{A}\,\overline{C}$

 $\mathsf{Y}=\overline{\mathsf{X}}$
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<u>No. 3</u>

- Connect Vcc to 5V
- Connect GND and Strobe to ground
- Connect D5, D10, and D14 to ground
- Connect all other D inputs to 5V

<u>No. 4</u>

No output line is active, chip is disabled \rightarrow Strobe is high!

<u>No. 5</u>

-R and T \rightarrow high -ABCD = 1001

-

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Preface

Nearly two years ago the German Development Service (DED) offered me the possibility to assist a technical college in the Philippines.

I had finished my studies in electronic engineering in Germany and had gained several years of working experience in the development of medical electronic equipment and the organization of telecommunication units.

Since I have been assigned with the Don Bosco Technical College, I have been teaching in electronics, computer science, and have been working in the training for instructors.

One of the mayor problems I encountered was the lack of preparation time for the lessons. Many teachers are under steady time pressure because they have to serve two or more jobs in order to earn the adequate income. That gave me the idea to develop a ready-made lesson preparation for teachers.

Based on my experience and also due to the visit of many other schools I edited and compiled this Teaching Aid. I tried to integrate practice and theory which is the best way to provide a solid foundation. I hope this will support the teachers as well as it can improve the quality of classes.

Canlubang, Philippines February 1994

Andreas Lange



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Third Evaluation Answers to Evaluation Problems

Introduction

This Teaching Aid is addressed to teachers and schools which offer any kind of electronic courses (i.e. computer maintenance, machine control, radio and tv repair, etc). It provides the basic knowledge for technicians as well as it can be used to run basic courses at technical colleges.

Digital Teaching Aid is a teaching module made for teachers. It is a ready - made lesson preparation and not a textbook. Therefore, you (the teacher) should already have some background knowledge on digital electronics. This module gives you all the material you need to run a course in basic digital electronics.

The module is divided into lessons, each lesson is headed by a lesson plan followed by boardscripts, worksheets, and handouts. It also contains three evaluations which you can use as tests/exams or as advanced exercises. The lesson plans are not only containing the contents of the lesson, but also gives you the objectives and suggested methods and ways to carry out the lesson. The following informs you about the purpose of every lesson plan column:

- Time The 'Time' column is still blank, it is up to you to decide how much time you would like to spend on each topic. The average time per lesson is approximately 90 minutes and 45 minutes for the review exercise (Worksheet).
- Method The 'Method' column suggests a sample of teaching methods. Lesson plan 1 and 2 are already filled up to give you an example on how to use this column. I

recommend the use of abbreviations, the meaning of every abbreviation is given at the bottom of every method column.

- Topic The 'Topic' column gives you a brief description of the contents of every lesson. Feel free to add or drop some topics. Every topic is handled in the following boardscript pages.
- Way The 'Way' column suggests a sample of teaching tools. Lesson plan 1 and 2 are already filled up. The explanation for the abbreviation used is given at the bottom of every way column. The boardscript pages of every lesson contain examples (EX) and hands on (HO) exercises. The HO's should be carried out by the students during the lesson.
- Remark The 'Remark' column provides you with space for additional information. (i.e.: Where can I find the transparency/picture which I decided to use, or: What is the filename of the demo program which I already prepared)





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Fundamental Logic Operations - Lesson 1

Lesson Plan

Titel: Fundamental Logic Operations

Objectives:

- Understand the principle of NOT, AND, OR operations
- Able to convert binary and decimal numbers

Time	Method	Торіс	Way	Remark
	S,D	* Introduction	Ex	
		- Analog and digital		

	signals		
S,Q/A	* Review	В	
	-Transistor in hard saturation		
	- Inverter function		
S,D	*TTL circuits	В	
	-History		
	- Standards		
S	* Logic operations	В	
S,E	-NOT	НО	Handout No. 1 (Family of TTL devices)
S,E	-AND	EX	
S,E	-OR	EX	
E	* Binary number system	WS	Worksheet No. 1
S: Speech D: Discussion Q/A: Question/Answer E: Exercise		B: Boardscript P: Picture Ex: Example HO: Hands- On WS: Worksheet	

Introduction

Fundamental Logic Operations

Digital Electronics

The world of electronics is divided into two areas: analog and digital. Analog circuits consist mainly of amplifiers for voltage or current variations that are smooth and continuous. Digital circuits provide electronic switching of voltage pulses. A pulse has abrupt changes between two extreme amplitude levels (i.e.: 5 volt = high level and 0 volt = low level).

Since the digital signal has only two significant levels, either high or low, it is useful to represent the pulses in a binary number system with the digits 1 and 0. (see also Worksheet 1, Binary number system)



Transistor in digital electronic

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A transistor can be used in analog and digital electronic. In digital electronic the transistor operates usually in hard saturation. (see also Amplifier Teaching Aid, Transistor as switch)



Fig. 1-2: Load line and circuit for a transistor switch

Hard Saturation

To get hard saturation, a designer makes \mathbf{I}_{C} approximately 10 times the value of $\mathbf{I}_{B}.$

When the max. Vin equals to the supply voltage you can get hard saturation by using a ratio of:

10:1 for R_B/R_C

Inverter Function

A transistor switch (circuit as above) can be used to build the first device in digital electronic, the inverter:



Fig. 1-3: Inverter symbol and truth table

Because in digital electronics mainly ready made devices are used (Integrated circuits IC), we don't care any more how the single device is built up. From now on we will use only these ready made devices.

TTL circuits

1964 TEXAS Instruments introduced a family of digital devices which became standard elements in digital electronic: The TTL (Transistor Transistor Logic) circuits. The High (1) and Low (1) state is represented by voltage levels.



Fig. 1-4: Voltage levels for high and low state in TTL IC's

Logic operations

All decisions and operations can be realized by means of the three basic operations:

NOT, AND, OR

NOT (Inverter)



Fig. 1-5: NOT (Inverter) symbol and truth table

<u>Circuit example:</u> 7404 TTL device (see Handout No. 1)

HO: A 1KHz square wave drives pin 1 of a 7404. What does the voltage waveform at pin 2 look like?

Solution:



AND gates

AND operation: The output supplies an high (1) signal if to all inputs high (1) signals are applied.



Fig. 1-6: AND symbol and truth table

<u>AND application example:</u> An elevator motor may only start to work if the doors are shut AND an operation occured.

<u>Circuit example:</u> TTL device 7408, two input AND gate

Ex: Develop the truth table for the following logic circuit.



OR gates

OR operation: An OR operation supplies a high signal at the output if to one or more inputs high signals are applied.



Fig. 1-9: OR gate, symbol and truth table

<u>OR application example:</u> A pump has to be switched on when the water level has fallen to a certain level OR too much water is taken out of the container.

<u>Circuit example:</u> TTL device 7432, two input OR gate

Ex: Develop the truth table for the following logic circuit.



Fig. 1-10: Logic circuit with truth table

Handout No. 1

The 7400 Family of TTL Devices (Sample List)

Device number	Description
7400	Quad 2 input NAND gates
7402	Quad 2 input NOR gates
7404	Hex inverter
7408	Quad 2 input AND gates
7410	Triple 3 input NAND gates
7411	Triple 3 input AND gates
7427	Triple 3 input NOR gates
7432	Quad 2 input OR gates

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Worksheet No. 1

Binary number system

All number systems have a base, which specifies how many digits can be used in each place count. For binary numbers the base is 2, with 0 and 1 as the only two digits. In the decimal system, the base is 10.

Decimal digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

Binary digits: 0, 1

Decimal to Binary Conversion



Each digit position has specified weight, for binary numbers the position represents a power of two.





HO: Convert the following binary numbers into decimal:

101, 1100, 1110, 1000, 0110, 11001010, 01101111, 10001100

Binary to decimal conversion



HO: Convert the following decimal numbers into binary numbers:

12, 8, 127, 247, 139, 255



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Introduction Boolean Algebra - Lesson 2

Lesson Plan

Introduction

Titel: Introduction Boolean Algebra

Objectives:

- Able to express the basic operations in Boolean algebra
- Know how to describe a logic circuit in a Boolean equation
- Understand the basic Boolean theorems.

Time	Method	Торіс	Way	Remark
	Q/A	* Review Lesson 1	В	
	S	* Introduction - George Boole	В	
	S	* Boolean algebra	B,Ex	
	S,E	- NOT operation		
		- OR operation		
		- AND operation		
	S,E	- Boolean equations of logic circuits	B,Ex	
		- NOR gates Truth table	В	
	S,D	- De Morgan's 1. theorem	В	
		- NAND gates Truth table	В	
	E	- De Morgan's 2. theorem	B,HO	
	E	* Review Exercise	WS	Worksheet No. 2
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	S. Sheerii		D. Duai usci ipu	
	D: Discussion		P: Picture	
	Q/A:		Ex: Example	
	Question/Answer		HO: Hands-	
	E: Exercise		On	
			WS:	
			Worksheet	
			HT: Hand-Out	

Boolean algebra

George Boole (1854) invented a new kind of algebra that could be used to analyse and design digital and computer circuits.

NOT operation



Fig. 2-1: Inverter symbol and Boolean notation

Ex: If A is 0 (low) \rightarrow X = NOT 0 = 1

In Boolean algebra the overbar stands for NOT operation.

 $X = \overline{A}$

OR operation



Fig. 2-2: OR symbol and Boolean notation

Ex: If A = 0, $B = 1 \rightarrow X = A$ or B = 0 or 1 = I

In Boolean algebra the + sign stans for the OR operation:

 $\mathbf{X} = \mathbf{A} + \mathbf{B}$

Ex: If A = 1, $B = 0 \rightarrow X = A + B = 1 + 0 = 1$

AND operation



Fig. 2-3: AND symbol and Boolean notation

In Boolean algebra the multiplication sign stands for the AND operation:

 $\mathbf{X} = \mathbf{A} \bullet \mathbf{B}$

or simply:

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X = A B

Ex: If A = 1, $B = 0 \rightarrow X = A B = 1 \cdot 0 = 0$

Boolean equations of logic circuits

You can use Boolean algebra as a shorthand notation for digital circuits.

<u>Ex:</u>



Output of the first gate:

X3 = A + B

Output of the second gate:

X6 = X3 + C = A + B + C

The final output is:

X8 = X6 + D = A + B + C + D = X

<u>HO</u>: Find the Boolean equation for the following circuit.



Fig. 2-5: Logic circuit

Solution:

X = (A + B) (C + D)

NOR and NAN gates

NOR gate

Based on the three fundamental logic operations it is possible to design additionel logic devices.





Formula: $\chi = \overline{A+B}$

NAND gate



Fig. 2-7: NAND grate, symbol and truth table

Formula: $\chi = \overline{A B}$

De Morgan's theorems

Augustus De Morgan was the first who found the link between logic and mathematics.

х





Fig. 2-8: Logic circuits with the same output

Although the circuits are different but the output, as we can see in the truth table, is equal. Therefore we can write:

 $\overline{A}\overline{B} = \overline{A+B}$

De Morgan's First Theorem

Also if we compare the two circuits on the next page we can easily see that the output is the same, although the circuits are different.

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Fig. 2-9: Logic circuits with the same output

1

0

0

1

So we can write:

 $\overline{AB} = \overline{A} + \overline{B}$

De Morgan's Second Theorem

1

HO: How can you connect a NAND gate to get an inverter

1





HO: How can you connect NAND gates to get an OR gate?

Solution:



Worksheet No. 2



No. 1 What is the Boolean equation? What is the truth table?



No. 2 What is the Boolean equation? What is the truth table?



No. 3 What is the Boolean equation? What is the truth table?



No. 4 Construct the truth table.

No. 5 Draw the logic circuit whose Boolean equation is

 $X = \overline{A + B} + \overline{C}$

Use the 7404 and the 7432 with pin numbers

No. 6 Draw the logic circuit whose Boolean equation is

 $X = \overline{ABC} - A\overline{BC}$

Use the 7404, 7432 and the 7411 with pin numbers.



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Circuit Analysis and Design - Lesson 3

Lesson Plan

Titel: Circuit Analysis and Design

Objectives:

- Know how to apply the basic Boolean laws
- Able to create digital circuits with the help of the sum of products method

Time	Method	Торіс	Way	Remark
		* Review Lesson 2		
		* Introduction		
		* Boolean laws and theorems	HO	Handout No. 2 (Boolean Algebra Theorems)
		- Basic laws		
		- Boolean relation about OR operations		
		- Boolean relations about AND operations		
		* Sum of products method		
		- Fundamental products		
		- Sum of products equations		
		* Review Exercise	WS	Worksheet No. 3
	S: Speech D: Discussion QA:		B: Boardscript P: Picture	

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	Question/Answer	Ex:	
	E: Exercise	Example	
		HO:	
		Hands-On	
		WS:	
		Worksheet	
		HT: Hand-	
		Out	

Introduction

Circuit Analysis and Design

Boolean laws and theorems

Basic laws

(see also Handout No. 2)

Commutative law:

 $\mathbf{A} + \mathbf{B} = \mathbf{B} + \mathbf{A}$

A B = B A


Associative law:

$$A + (B + C) = (A + B) + C$$

A (B + C) = (A B) C



Distributive law:

A (B + C) = AB + AC



Boolean relations about OR operations

$$\mathbf{A} + \mathbf{0} = \mathbf{A}$$

Proof:

when A is 0 0 + 0 = 0when A is 1 1 + 0 = 1A + A = A**Proof:** when A is 0 0 + 0 = 0when A is 1 1 + 1 = 1A + 1 = 1

Proof:

when A is 0

0 + 1 = 1

when A is 1

1 + 1 = 1

 $\mathbf{A} + \mathbf{A} = \mathbf{1}$

If one input is high, the output is high no matter what the other input is.

Boolean relations about AND operations

 $A \bullet 1 = A$ $A \bullet A = A$ $A \bullet 0 = 0$

HO: Check the equations above in the same way as we did it before.

 $\mathbf{A} \bullet \mathbf{A} = \mathbf{0}$

If one input is low, the output is low no matter what the other input is.

Double inversion

= A = B

De Morgan's theorems

 $\overline{A+B}=\overline{A}\overline{B}$ see also Lesson 1

 $\overline{A+B} = \overline{A}B$

Duality theorem

- 1. Change each OR sign to an AND sign
- 2. Change ech AND sign to an OR sign

3. Complement any 0 or 1 appearing in the expression

Ex: A + 0 = A $\rightarrow A 1 = A$ Ex: A (B + C) = AB + AC $\rightarrow A + B C = (A + B) (A + C)$

TIP: Proof it with a truth table

Ex: Simplify the following Boolean equation

 $X = A\overline{B} + AB$

Solution: (see also Handout No. 2)

 $\begin{array}{ll} \mathsf{X} = \mathsf{A}(\overline{\mathsf{B}} + \mathsf{B}) \ \textit{Handout 2 No. 3a} \\ \mathsf{X} = \mathsf{A} \ (1) & \textit{No. 8a} \\ \mathsf{X} = \mathsf{A} & \textit{No. 7b} \end{array}$

<u>HO</u>: Simplify the following Boolean equation

$X = (\overline{A} + B)(A - B)$

Solution:

 $X = \overline{A}A + \overline{A}B + BA + BB$ $X = \overline{A}B + BA + B$ $X = (\overline{A} + A)B + B$

X = B + BX = B

Sum of product method

Fig. 3-4: Example truth table with fundamental products

A	B	X	Fundamental Products
0	0	0	ĀĒĊ
0	0	1	ĀĒC
0	1	0	ĀBĒ
0	1	1	ĀBC
1	0	0	ABC
1	0	1	ABC
1	1	0	ABC

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Design example

Sum of products equation

Given is the following truth table:

Fig. 3-5: Example truth table



We have to locate each output 1 in the truth table and write down the fundamental product.

The next step is to OR the fundamental products:

 $X = \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC}$

Now we can derive the corresponding logic circuit:



Fig. 3-6: Logic circuit

HO: What is the sum of product circuit for the given truth table?

Fig. 3-7: Truth table





Handout No. 2

Boolean Algebra Theorems

No	Theorem	Name
1a 1b	A + B = B + A $AB = BA$	Commutative law
2a 2b	(A + B) + C = A + (B + C) (AB) C = A (B + C)	Associative law
3a 3b	A (B + C) = AB + AC A + (BC) = (A + B) (A + C)	Distributive law
4a 4b	A + A = A $AA = A$	Identity law
5a 5b	$\overline{A} = \overline{A}$	Negation

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6a 6b	$\overline{A} = A$ A (A + B) = A	Redundancy
7a	$0 + \mathbf{A} = \mathbf{A}$	
7b	$1 \mathbf{A} = \mathbf{A}$	
7 c	1 + A = 1	
7 d	$\mathbf{OA} = \mathbf{O}$	
8 A	$\overline{A} + A = 1$	
8b	ĀA=0	
9a	$A + \overline{AB} = A - B$	
9c	$A(\overline{A}-B)=AB$	
10a	$\overline{A+B} = \overline{A}\overline{B}$	De Morgan's laws
10b	$\overline{AB} = \overline{A} + \overline{B}$	_

Worksheet No. 3

No. 1 Simplify the Boolean equation and discribe the logic circuit:

 $\overline{ABC} + \overline{ABC} + \overline{ABC} - \overline{ABC} = X$

No. 2 Simplify the following Boolean expressions:

 $\overline{A}\overline{B} + AB + \overline{A}B$ (A + B)(A + \overline{B}) $\overline{A}B + A\overline{B} + AB + \overline{A}\overline{B}$ No. 3 A digital system has a 4-bit input from 0000 to 1111. Design a logic circuit that produces a high output whenever the equivalent decimal input is greater than 13.

<u>No. 4</u> In a heating plant the burner X has to be switched on, when the circulating pump A is actuated and the temperature probe B for the warm water supply or the room temperature probe C respond.

- a) Develop the truth table
- b) Write down the sum of products equation
- c) Draw the logic circuit
- d) Use Boolean algebra to simplify the equation
- e) Draw the corresponding logic circuit.





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- (introduction...)
- Preface
- Introduction
- Fundamental Logic Operations Lesson 1
- □ Introduction Boolean Algebra Lesson 2
- □ Circuit Analysis and Design Lesson 3
- **First Evaluation**

- Karnaugh Mapping Lesson 4
 Karnaugh Mapping II Lesson 5
- □ Coding Lesson 6
- Flip-Flops Lesson 7
- Second Evaluation
- Counter Lesson 8
- Data Processing Circuits Lesson 9
- Third Evaluation
- Answers to Evaluation Problems

First Evaluation

No. 1 Construct the truth Table

What is the Boolean equation?



No. 2 Draw the logic circuit whose Boolean equation is

$$X = \overline{(ABC)}\overline{D}$$

Use the 7404, 7408 and the 7411 with pin numbers

No. 3 Simplify the following Boolean expressions

 $ABC + \overline{AB} + AB\overline{C}$ ABC + AC $\overline{(A + B)}(\overline{A} + \overline{B})$

No. 4 A digital system has a 4 bit input from 0000 to 1111.

Design a logic circuit that produces a high output whenever the equivalent hex input is greater than C.

Truth table

Sum of products equation

Logic circuit

<u>No. 5</u>



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0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

- a) Draw the Karnaugh map
- b) Encircle all octets, quads, and pairs you can find.
- c) What is the simplified Boolean equation?
- d) Draw the logic circuit using NAND gates.



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- ➡□ Karnaugh Mapping Lesson 4
 - Lesson Plan



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(introduction...)

Introduction

Karnaugh map

Truth table to Karnaugh map

- Pairs, Quads, and Octets
- Overlapping and Rolling

Worksheet No. 4

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Karnaugh Mapping - Lesson 4

Lesson Plan

Titel: Karnaugh Mapping

Objectives:

- Able to derive Karnaugh maps from a given truth table
- Know how to simplify Karnaugh maps

Time	Method	Торіс	Way	Remark
		* Review Lesson 3		
		* Introduction		
		- Karnaugh man		

	* Karnaugh mapping		
	- Truth table to Karnaugh		
	map		
	- Two variable map		
	- Three variable map		
	- Four variable map		
	- Pairs, Quads, and Octets		
	- Overlapping groups		
	- Rolling the map		
	* Review exercise	WS	Worksheet No.
			4
S: Speech		B: Boardscript	
D Discussion		P: Picture	
Q/A:		Ex: Example	
Question/Answer		HO: Hands-On	
E: Exercise		WS:	
		Worksheet	
		HT: Hand-Out	

Introduction

Karnaugh Mapping

E

Simplify a Boolean equation

x:	$X = \overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + A\overline{B}\overline{C} + A\overline{B}\overline{C}$	
	$X = \overline{C}(\overline{A}\overline{B} - \overline{A}B + A\overline{B} + AB)$	\overline{c} is common in each term
	$X = \overline{C}[(\overline{A}(\overline{B}+B)+A(\overline{B}+B)]$	Again factor to get
	$\mathbf{X} = \overline{\mathbf{C}} \left[\overline{\mathbf{A}}(1) + \mathbf{A}(1) \right]$	Simplify
	$X = \overline{C}(\overline{A} + A)$	Simplify
	$X = \overline{C}$	

Karnaugh map

As you see, Boolean algebra can be used to create simpler circuits. But if you not quite familiar with Boolean theorems it is difficult to find the best simplification. Therefore Karnaugh mapping is the better alternative for simplification.

Truth table to Karnaugh map

The starting point for digital circuit design is usually the truth table which gives us the following information:

Under which input condition occurs a certain output condition.

Two variable map



Fig. 4-1: Two variable Karnaugh map

The truth table outputs are translated into the Karnaugh map. Each position in the map represents a certain fundamental product.

Three variable map

Ex:

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Four variable map

Many digital systems process 4 bit numbers. For this reason, logic circuits are often designed to handle 4 input variables.

Ex:

(see Fig. 4-3)



Fig. 4-3: Four variable Karnaugh map

Pairs, Quads, and Octets

Pairs



Digital Teaching Aid (DED Philippinen, 86 p.) **Fig. 4-4: Four variable simplification**

As you see in Fig. 4-4, only one variable goes from uncomplement to complement. Whenever this happens, you can eliminate the variable that changes form.

Proof: $X = ABCD + ABC\overline{D}$ $X = ABC(D + \overline{D})$ X = ABC

Ex:



Whenever you see a pair first encircle it and then simplify to get the simplified Boolean expression:

 $X = A\overline{C}\overline{D} + \overline{A}BD$

Quad





Quad: A group of 4 one's that are horizontally or vertically adjacent. End to end or in form of a square.

A quad eliminates two variables and their complements.

Proof: $X = AB\overline{C} + ABC$ (two pairs) X = A B (C + C)X = A B

Encircle the quad and step through the different one's in the quad and determine which two variables go from complement to uncomplement (or vs), these are the variables that drop out.

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The variables B and D can be eliminated. So we get the following equation:

 $\mathbf{X} = \mathbf{A} \mathbf{C}$

Octet



An octet eliminates three variables and their complements.

Proof: $X = A\overline{C} + AC$ (two quads) X = A (C + C)X = A

Karnaugh Simplifications

Process:

- 1. Draw the Karnaugh map
- 2. Look for octets and encircle them.
- **3. Look for quads and encircle them.**
- 4. Look for pairs and encircle them.
- 5. Simplify and write down the equation.



 $X = A\overline{C} - C\overline{D} + \overline{A}BD$

Overlapping and Rolling

Overlapping groups





Groups can overlap to get a simpler equation:

 $X = A + B\overline{C}D$

Rolling the map



Fig. 4-11: Karnaugh map

Instead of encircling two pairs:

 $X = B\overline{C}D - BC\overline{D}$

We can roll the map and encircle a quad:

 $X = B\overline{D}$



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Solution:

 $X = \overline{C} + \overline{A}\overline{D} + A\overline{B}D$



Solution:

X = AB + AD + AC + BCD

Worksheet No. 4

<u>No. 1</u> Simplify the following Karnaugh maps and write down the Boolean equation for every map.









	ĒD	ĒD	CD	CD
$\bar{A}\bar{B}$	0	1	0	0
ĀΒ	1	0	1	1
AB	1	0	0	1
$A\bar{B}$	0	1	1	0

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	ĒD	СD	CD	CD
$\bar{A}\bar{B}$	1	1	0	1
$\overline{A}B$	0	0	1	1
AB	0	0	0	1
$A\bar{B}$	1	1	0	1

<u>No. 2</u> Translate each output (v, w, x, y, z) into a Karnaugh map, do the simplification and write down the Boolean equation.

Π									
	A	B	C	D	V	W	X	Y	Z
	0	0	0	0	1	1	0	1	0
	0	0	0	1	0	1	0	1	1
	0	0	1	0	0	1	0	0	0
	0	0	1	1	0	0	0	0	1
	0	1	0	0	0	0	1	0	1
	0	1	0	1	1	0	1	1	0
	0	1	1	0	1	1	1	1	0
	0	1	1	1	1	0	1	1	0
	1	0	0	0	0	1	0	0	1
	1	0	0	1	1	1	1	1	0
	1	0	1	0	0	1	0	1	0
	1	0	1	1	1	1	1	1	1
	1	1	0	0	0	0	0	0	1
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1	Ĺ			<u> </u>		<u> </u>			
	1	1	0	1	1	0	0	0	1
	1	1	1	0	0	0	0	1	1
	1	1	1	1	0	1	0	0	0





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 Karnaugh Mapping II - Lesson 5

 Lesson Plan
 (introduction...)
 Introduction
 Product of sums method
 Don't care conditions
 Worksheet No. 5

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Karnaugh Mapping II - Lesson 5

Lesson Plan

Titel: Karnaugh Mapping II

Objectives:

- Understand the product of sums method
- Able to use "Don't care conditions" for more effective simplifications

Time	Method	Торіс	Way	Remark
		* Review Lesson 4		
		* Introduction		
		* Product of sums method		
		- Fundamental sums		
		- Product off sums simplifications		
		* Don't care conditions		
		-Truth table		
		- Karnaugh map		
		* Review exercise		Worksheet No. 5
	S: Speech D: Discussion Q/A: Question/Answer E: Exercise		B: Boardscript P: Picture Ex: Example HO: Hands-On WS: Worksheet HT: Hand-Out	

Introduction

Karnaugh Mapping II

Product of sums method

Instead of using the sum of products method we can also take the product of sums method which is based on the fundamental sums:

Fig. 5-1: Truth table with fundamental sums

A	B	C	X		Fundamental sums
0	0	0	0	\rightarrow	A+B+C
0	0	1	1		
0	1	0	1		
0	1	1	0	\rightarrow	$A + \overline{B} + \overline{C}$
1	0	0	1		
1	0	1	1		
1	1	0	0	\rightarrow	$\overline{A} + \overline{B} + C$
1	1	1	1		

Product of sums simplification

A equation gained through the sum of product method can be realized into a

NAND-NAND logic circuit.



Fig. 5-2: NAND-NAND logic circuit

If we simplify the Karnaugh map in Fig. 5-2 we get the following equation:

 $X = \overline{A}\overline{B} + AB + AC$

Based on this equation we can draw the logic circuit like in Fig. 5-2. This solution is made with the help of the sum of product method. If we want to try the product of sums method we have to go through the following steps:

1. Complement the Karnaugh map and draw the complementary NAND-NAND circuit:

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Fig. 5-3: Complementary NAND-NAND circuit

The simplified equation is:

 $\overline{X} = \overline{A}B + A\overline{B}\overline{C}$

2. Convert the complementary NAND-NAND circuit to a NOR-NOR circuit:



we have changed all NAND to NOR and complemented all signals.

3. Now we got a product of sums solution for X. The last step is to compare both circuits (NAND-NAND, NOR-NOR) to find out which circuit is the simpler one, meaning the cheaper one. Because we need less gates. In our case the sum of product solution (NOR-NOR circuit) is the better solution.

Summary of process

1. Convert the truth table into a Karnaugh map

- Write the sum of products equation
- Draw the NAND-NAND circuit
- 2. Complement the Karnaugh map
 - Draw the complementary NAND-NAND circuit (\overline{X})
- **3.** Convert the complementary NAND-NAND circuit to a NOR-NOR circuit.
 - Change all NAND to NOR
 - Complement all signals
- 4. Compare NAND-NAND circuit with NOR-NOR circuit.

Don't care conditions

In some digital systems, certain input conditions never occur during normal operations; therefore, the corresponding output never appears.

\Rightarrow It is indicated in the truth table by an X.

Fig. 5-5: Don't care conditions

A	B	C	D	Z	
0	0	0	0	0	
0	0	0	1	0	
0	0	1	0	0	
0	0	1	1	0	
0	1	0	0	0	
0	1	0	1	0	
0	1	1	0	0	
0	1	1	1	0	
1	0	0	0	0	
1	0	0	1	1	
1	0	1	0	X	
1	0	1	1	X	
1	1	0	0	X	Don't care conditions
1	1	0	1	X	
1	1	1	0	X	
1	1	1	1	X	

Don't care conditions are like wild cards, you can let them stand for what ever you
^{21/10/2011} **like:**

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Fig. 5-6: Karnaugh map and simplified equation

HO: Simplify the following Boolean function:

 $F(w,x,y,z) = \Sigma(1,3,7,11,15)$

That has the don't care conditions:

 $d(w,x,y,z) = \Sigma(0.2,5)$

Solution:

First we have to translate the function into a truth table:

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	W	X	Y	Ζ	F
	0	0	0	0	X
	0	0	0	1	1
	0	0	1	0	X
	0	0	1	1	1
	0	1	0	0	0
	0	1	0	1	X
	0	1	1	0	0
	0	1	1	1	1
	1	0	0	0	0
	1	0	0	1	0
	1	0	1	0	0
	1	0	1	1	1
	1	1	0	0	0
	1	1	0	1	0
	1	1	1	0	0
	1	1	1	1	1

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Now we have to convert it into a Karnaugh map and simplify it:

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Worksheet No. 5

<u>No. 1</u>



21/10/2011



- a) Draw the Karnaugh map.
- b) Encircle all octets, quads and pairs you can find.
- c) What is the simplified Boolean equation for the Karnaugh map?
- d) Draw the logic circuit.

e) Suppose the last six entries of the truth table are changed to don't cares. Using the Karnaugh map, show the simplified circuit.

f) What is the simplified NOR-NOR circuit?

