Patent Application

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Title:

A method for determination of an exception in multi-dimensional data

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A B S T R A C T

A method for determination of an exception in multidimensional data, the method comprising the steps of:

- a) determination of an expected value for a set of cells of the multi-dimensional data by means of an ANOVA based method,
- b) determination of a residual for each cell of the set of cells,
- c) scaling of the residuals,
- d) comparing the scaled residuals with a threshold value for determination of the exception.

(Fig. 2)

DESCRIPTION

A method for determination of an exception in multi-dimensional data

FIELD OF THE INVENTION

The present invention is related to an improved data processing system. A more particular aspect of the present invention is related to the application of decision support techniques such as online analytical processing (OLAP) to databases.

BACKGROUND

Decision support is rapidly becoming a key technology for business success. Decision support allows a business to deduce useful information, usually referred to as a data warehouse, from an operational database. While the operational database maintains state information, the data warehouse typically maintains historical information. Users of data warehouses are generally more interested in identifying trends rather than looking at individual records in isolation. Decision support queries are thus more computationally intensive and make heavy use of aggregation. This can result in long completion delays and unacceptable productivity constraints.

Some known techniques used to reduce delays are to pre-compute frequently asked queries, or to use sampling techniques, or both. In particular, applying online analytical processing (OLAP) techniques such as data cubes on very large relational databases or data warehouses for decision support has received increasing attention recently (see e.g., Jim Gray, Adam Bosworth, Andrew Layman, and Hamid Pirahesh, "Data Cube: A Relational Aggregation Operator Generalizing Group-By, Cross-Tab, and Sub-Totals", International Conference on Data Engineering, 1996, New Orleans, pp. 152-160) ("Gray"). Here, users typically view the historical data from data warehouses as multidimensional data cubes. Each cell (or lattice point) in the cube is a view consisting of an aggregation of interests, such as total sales.

Commonly encountered aggregation queries for data warehouse applications include those already defined in the standard Structured Query Language (SQL).

Relational DataBase Management System (RDBMS) software using a Structured Query Language (SQL) interface is well known in the art. The SQL interface has evolved into a standard language for RDBMS software and has been adopted as such by both the American National Standards Institute (ANSI) and the International Standards Organization (ISO).

RDBMS software has typically been used with databases comprised of traditional data types that are easily structured into tables. However, RDBMS products do have limitations with respect to providing users with specific views of data. Thus, "frontends" have been developed for RDBMS products so that data retrieved from the RDBMS can be aggregated, summarized, consolidated, summed, viewed, and analyzed. However, even these "front-ends" do not easily provide the ability to consolidate, view, and analyze data in the manner of "multi-dimensional data analysis." This type of functionality relies on OLAP.

OLAP generally comprises numerous, speculative "what-if" and/or "why" data model scenarios executed by a computer. Within these scenarios, the values of key variables or parameters are hanged, often repeatedly, to reflect potential variances in measured data. Additional data is then synthesized through animation of

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the data model. This often includes the consolidation of projected and actual data according to more than one consolidation path or dimension.

Data consolidation is the process of synthesizing data into essential knowledge. The highest level in a data consolidation path is referred to as that data's dimension. A given data dimension represents a specific perspective of the data included in its associated consolidation path. There are typically a number of different dimensions from which a given pool of data can be analyzed. This plural perspective, or Multi-Dimensional Conceptual View, appears to be the way most business persons naturally view their enterprise. Each of these perspectives is considered to be a complementary data dimension. Simultaneous analysis of multiple data dimensions is referred to as multidimensional data analysis.

OLAP functionality is characterized by dynamic multi-dimensional analysis of consolidated data supporting end user analytical and navigational activities including:

calculations and modeling applied across dimensions, through hierarchies and/or across members;

trend analysis over sequential time periods;

slicing subsets for on-screen viewing;

drill-down to deeper levels of consolidation;

reach-through to underlying detail data; and rotation to new dimensional comparisons in the viewing area.

OLAP is often implemented in a multi-user client/server mode and attempts to offer consistently rapid response to database access, regardless of database size and complexity.

Corresponding OLAP database systems are known for example from US-A-6205 447, US-A-6122 636, US-A-5978 796, US-A-5978 788 and US-A-5940 818.

In essence, OLAP software enables users, such as analysts, managers and executives, to gain insight into performance of an enterprise through rapid access to a wide variety of data views that are organized to reflect the multidimensional nature of the enterprise performance data. An increasingly popular data model for OLAP applications is the multidimensional database (MDDB), which is also known as the data cube. OLAP data cubes are predominantly used for interactive exploration of performance data for finding regions of anomalies in the data, which are also referred to as exceptions or deviations. Problem areas and/or new opportunities are often identified when an anomaly is located.

To create an MDDB from a collection of data, a number of attributes associated with the data are selected. Some of the attributes are chosen to be metrics of interest and are each referred to as a "measure," while the remaining attributes are referred to as "dimensions." Dimensions usually have associated "hierarchies" that are arranged in aggregation levels providing different levels of granularity for viewing the data.

Exploration typically begins at the highest level of a dimensional hierarchy. The lower levels of hierarchies are then "drilled-down" to by looking at the aggregated values and visually identifying interesting values within the aggregated values. For example, drilling-down along a product dimension from a product category to a product type may identify product

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types exhibiting an anomalous sales behavior. Continued drilldown from the product type may identify individual products causing the anomalous sales behavior. If exploration along a particular path does not yield interesting results, the path is "rolled-up" and another branch is examined. A roll-up may return to an intermediate level for drilling-down along another branch, or the top-level of the hierarchy may be returned to and another drill-down may continue along another dimension.

Besides being cumbersome, this "hypothesis-driven" exploration for anomalies has several shortcomings. For example, the search space is usually large-a typical data cube has 5-8 dimensions with any particular dimension having hundreds of values, and each dimension having a hierarchy that is 3-8 levels high, as disclosed by George Colliat, OLAP, relational, and multidimensional database systems, Technical report, Arbor Software Corporation, Sunnyvale, Calif., 1995. Consequently, an anomaly can be hidden in any of several million values of detailed data that has been aggregated at various levels of detail. Additionally, higher level aggregations from where an analysis typically begins may not be affected by an anomaly occurring below the starting level because of cancellation effects caused by multiple exceptions or simply by the large amount of aggregated data. Even when data is viewed at the same level of detail as where an anomaly occurs, the exception might be hard to notice.

What is needed is a way for conveniently performing an exploration of a data cube that ensures that abnormal data patterns are not missed at any level of data aggregation, regardless of the number of dimensions and/or hierarchies of the data.

US-A-6,094,651 shows a "discovery-driven" approach for data exploration of a data cube where a search for anomalies is

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guided to interesting areas of the data by pre-mined paths that are based on exceptions found at various levels of data aggregation. Consequently, it is ensured that abnormal data patterns are not missed at any level of data aggregation, regardless of the number of dimensions and/or hierarchies of the data by providing a paradigm of pre-excavated exceptions.

Further, this provides a method for navigating large multidimensional OLAP datasets for locating exceptions, and for guiding a user to interesting regions in a data cube using premined exceptions that exhibit anomalous behavior. The number of drill-downs and selection steps is significantly reduced in comparison to other conventional approaches for manually finding exceptions, especially in large data cubes having many different dimensions and hierarchies.

Data anomalies in a k dimensional data cube are identified by the steps of associating a surprise value with each cell of a data cube, and indicating a data anomaly when the surprise value associated with a cell exceeds a predetermined exception threshold.

It is an object of the invention to provide an improved method for determining an exception in multidimensional data and to provide a corresponding computer system and computer program product.

SUMMARY OF INVENTION

The object of the invention is solved by applying the features of the independent claims.

Preferred embodiments of the invention are set forth in the dependent claims.

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The present invention provides an efficient and accurate method for determination of exceptions in multi-dimensional data, such as multi-dimensional data in an OLAP data base. In accordance with the present invention the determination of exceptions relies on multivariate data analysis, and in particular the ANOVA method.

The ANOVA method is as such known from "Applied multivariate data analysis", J. D. Jobson., Springer Verlag, ISBN 0387-97660-4.

There are a number of variants of the ANOVA method such as ANOVA based on a linear model and based on a log-linear model.

The application of the log-linear ANOVA method provides good results but is only applicable for positive data values whereas the linear ANOVA method has no restrictions as far as the data value range is concerned and can also be employed for negative data values but has an inferior accuracy.

In a preferred embodiment of the invention the multi-dimensional data is transformed by means of a variance stabilization transformation prior to the application of an ANOVA method. For example this can be accomplished by applying a non-linear transformation function having a larger slope for small data values and for large data values to accomplish a weighting function.

After the transformation preferably a linear ANOVA based method is applied in order to determine exceptions. This results in a method providing highly accurate results without a limitation as to the range of data values. In particular the method can also be employed for negative data values.

It is a further advantage of the invention that it enables a user to determine an exception within a user specified aggregate

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level. This enables the user to get answers for business questions related to the selected sub-cube of the OLAP database as defined by the user.

In the following a preferred embodiment of the invention is explained in greater detail with respect to the drawings in which

- Fig. 1 is illustrative of a first embodiment of a method in accordance with the invention,
- Fig. 2 is illustrative of a second embodiment of a method in accordance with the invention,
- Fig. 3 shows an example of a cube of an OLAP data base,
- Fig. 4 shows an example for an exception list,
- Fig. 5 shows an example for an exception in the context of an OLAP cube,
- Fig. 6 shows a further example in the context of an OLAP cube,
- Fig. 7 shows an example for an exception for a user defined aggregate level.

Fig. 1 shows a first embodiment for finding an exception in multi-dimensional data stored in an OLAP data base.

In step 10 an expected value is calculated for all cells within a given OLAP cube. The expected values are calculated by means of an ANOVA based method. A variety of ANOVA based methods for calculation of the expected values is explained in greater detail in the mathematical appendix. In step 12 the residuals are calculated for all cells of the OLAP cube. This is done by determining the difference between the actual observed data value of a cell i and the corresponding expected value as determined in step 10.

In step 14 the residuals determined in step 12 are scaled. This is done by calculating the standard deviation of the residuals from all cells comprised within the same aggregation level.

The residual i of a cell i of this aggregation level is standardized by dividing the residual i as determined in step 12 by the standard deviation of residuals for that aggregation level.

In step 16 it is decided whether the standardized residual i is greater than a threshold value. If this is not the case this means that the corresponding cell i does not contain an exception (step 18).

If the contrary is the case an output operation is performed in step 19 to highlight the exception to a user. Step 16 is performed with respect to all cells i in order to find exception within the cells i.

For example a threshold value of 2,5 is an advantageous choice but other threshold values can be chosen depending on the application. If a higher threshold value is chosen for step 16 only the strongest exceptions are identified as exceptions.

Fig. 2 shows an alternative embodiment of the method of Fig. 1. In step 11 a variance stabilization transformation is carried out for a transformation of data values of all cells i of a given OLAP cube or only a sub-set of the cells - depending on a user's choice. For example, a user can chose one or more

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interval ranges of cells to be transformed; in this case the other cells are ignored for the further processing.

In essence the variance stabilization transformation serves to limit the weight of large data values. This can be done by means of a non-linear transformation function having a slope greater than a constant C for an interval between a lower value $-x_s$ and an upper boundary value $+x_s$ and having a slope lesser than the constant C outside this interval.

An example for a function fulfilling these requirements is the function g(x) as shown in step 11 of Fig. 2. This function is symmetrical and has an unlimited data range for the argument x also spanning negative values for x.

The expected values for the cells are calculated by means of a linear ANOVA based method similar to step 10 of Fig. 1.

The consecutive steps 12 to 19 of Fig. 2 correspond to the steps having the same reference numerals of Fig. 1.

It is to be noted that the variance stabilization transformation is advantageous in that it provides results for the determination of an exception which are accurate and at the same time are not limited as far as the data range is concerned.

A comparison of the three ANOVA based approaches (linear model, log-linear model and linear model with variance stabilization transformation) shows the advantages of the different models.

For comparison of the three approaches reference is made to the exemplary cube 1 of Fig. 3 of an OLAP data base.

The cube 1 only contains positive cell values for purposes of the comparison, because the log-linear model is restricted to positive values.

The cube 1 is two dimensional; all cell values are equal to 2 except one row where cell values are 800 except a single cell of this row, which has the value 2. In addition the cube 1 contains one cell outside this row with a value of 9900. The cube has no aggregation levels.

The linear ANOVA model approach identifies only the 9900 cell as an exception. The log-linear model as well as the linear model with variance stabilization transformation identify the 9900 cell and the cell having the value of 2 within the 800 row (..., 800, 2, 800, ...) as exceptional. This example shows the drawbacks of the linear model approach without prior variance stabilization transformation where the extreme value of the exceptional cell 9900 hides all other exceptions.

Fig. 4 is illustrative of an application of the present invention to the field of banking. An OLAP cube out of the banking data area is selected in order to identify an exception. The banking cube consists of the dimensions Scenario, Product, Business unit, Individual age group, Customer relation ship, Customer annual income and a Time period. The Scenario (Actual) and the measure Profit are selected). The Fig. 4 shows the result of an examination run in accordance with the present invention which contains an exception list ranked in a descending order. The right most column of the table of Fig. 4 shows the magnitude of the scaled residuals.

Fig. 5 shows an example for an exception in the positive value range. It is to be noted that in the following sections the following definitions for hierarchies and their members are used:

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Definition 1: hierarchy name (member name) and Definition 2: hierarchy name (complete dimension) for complete dimensions.

One of these exceptions are selected and the result is shown in the context of an OLAP cube in Fig. 5. The exception 252.99 in MAR 1999 in the north region for the scenario (actual), the product (regular checking), the individual age group (31 to 45), customer relation ship (between 5 and 10 eared), the customer annual income (under \$ 20.000,00) is highlighted.

Fig. 6 shows an example for an exception in the positive and negative value ranges.

Again one of these exceptions is selected and the result is shown in the context of the OLAP cube. As a result there is an exception with a negative cell value -56.14 in MAR 1999 in the individual age group (31 to 45) for the scenario (actual), the product (regular checking), the business unit geography (complete dimension), the individual age group(31 to 45), customer relation ship (complete dimension), the customer annual income (\$ 60.000,00 to \$ 79.999,00). Further there is an exception at the same slice of the OLAP cube in the positive value range for the individual age group (65 and over) with the cell value 46.23 in column D, line 14 of Fig. 6.

It is most noticeable that the present invention enables the calculation of the standard deviations taking into account all selected cells in the same aggregation level of the OLAP cube. This type of calculation enables to provide answers to business questions related to the user selected sub-cubes.

In the following it is assumed that a user has the following two business questions with respect to the same OLAP cube:

- Is there an exception, if the profits of three products (A, B, C) in the last quarter (October, November, December) are compared?
- Is there an exception, if the profits of the three products (A, B, C) are compared for all quarters?

The result for the second question is shown in Fig. 7. Six deviations in columns C, D, lines 2, 3 and 4 are identified.

However no exceptions are identified for the first business question. It is to be noted that the same cells which deliver six deviations with respect to the second question to not show any exception in the first scenario.

In general terms exception or deviation detection aims to identify a singular real world pattern by using highly sophisticated models to describe the real world behavior. Because of many dependencies the real world behavior is often so complex that a deviation detection algorithm can only describe a sub-set of this behavior. Therefore it is important to understand which type of pattern can be identified by using a certain type of model. The more pattern can be identified, the more a certain method satisfies the customer needs. In accordance with the present invention a list of patterns is given in the following by way of example:

- 1. Exception on level 0 zero data which is the lowest aggregation level.
- 2. Exceptions in positive and negative value ranges (in this case a variance stabilization transformation is used).

- 3. Exceptions in data where the range of the existing values is very broad; again a variance stabilization transformation is used. Because of the weighting higher values do not overrule or "cover" smaller values.
- 4. Exceptions of time series patterns where the variance trespass the standard variation of the residuals.
- 5. Exceptions of aggregation levels which are based on exceptions on lower aggregation levels.
- Exceptions which only occur on aggregation levels where the level 0 data do not show any exception.
- 7. Exceptions which are dependent on the selected sub-cube. When the sub-cube is changed the associated exceptions change as well because the related business questions were also changed.

In particular the patterns 5 and 6 are very significant with respect to the multi-dimensional approach. One of the most important functions of a multi-dimensional data representation are the dynamic aggregations of these data and therefore it is highly desirable for any method for finding deviations / exceptions that it is able to support at least pattern 5 and / or preferably also pattern 6.

Further it is to be noted that instead of using a single variance stabilization transformation for all data partial transformations can be used for various interval ranges of the data values. For example a customer might be interested only in its negative appropriate measures. In this case the transformation function transforms the positive profits to 0. Further a customer might be interested only in profit measures which are in the range between 1000 and 2000. Therefore all values outside this interval are treated either as missing or will be transformed to a certain constant K, where K can be the mean of the interval between 1000 and 2000 or any other constant number.

Further, a customer might be interested in multiple intervals. In this case the values outside of these intervals are treated as mentioned above.

As a further example a customer might be interested in multiple intervals, where each interval is transformed by means of a separate variance stabilization transformation.

Mathematical Appendix

1. The ANOVA based linear model The two-way linear model for an expected value \bar{y}_{ijh} for a cell in the *i'th* row and the *j'th* column, with an error ε and cobservations is given by

$$i = 1, 2, ..., b;$$

 $\bar{y}_{ijh} = \mu + a_j + \beta_i + \varepsilon_{ijh}$ with $j = 1, 2, ..., g;$ (eq. 1)
 $h = 1, 2, ..., c.$

where μ denotes the true average over all cells. Introduce the following constraints

$$\sum_{i=1}^{b} \beta_{i} = \sum_{j=1}^{g} a_{j} = 0 \qquad (eq. 2)$$

and the model can be written as

$$i = 1, 2, ..., b;$$

 $\bar{y}_{ijh} = \mu_{ij} + c_{ijh} \text{ with } j = 1, 2, ..., g;$ (eq. 3)
 $h = 1, 2, ..., c.$

Assume the number of observations c=1

 $\mu_{ij} = \mu + a_j + \beta_i$ $a_j = \mu_{,j} - \mu$ $\beta_i = \mu_{i.} - \mu$

and hence

 $\mu_{ij} = \mu_{,j} + \mu_{i.} - \mu$

 $\mu_{ij} = \mu + (\mu_j - \mu) + (\mu_i - \mu)$. This results in

(eq. 4)

there the expected value \bar{y}_{ij} is expressed as sum of

- μ_{j} = mean of the cells in the *i'th* row
- μ_j = mean of the cells in the j'th column

• minus μ = overall mean of all cells

This approach can be enhanced for three-way, four-way and n-way models.

This ANOVA based approach can be adapted to OLAP cubes. For an observed value $y_{i_li_2...i_n}$ in a Cube G at position i_p of the p'fhdimension δ_p the expected value $\bar{y}_{i_li_2...i_n}$ is defined as function for the various aggregation levels with $g=2^n-1$ as:

$$\bar{y}_{i_1i_2\dots i_n} = \sum_{G \subset \{\delta_1 \delta_2 \dots \delta_n\}}^{g} \mu^{G}_{(i_p; \delta_p \in G)}$$
 (eq. 5)

Let us consider a cube with three dimension A,B,C. For the expected value \bar{y}_{ijk} for the *i'th* member of dimension A, the *j'th* member of dimension B and the *k'th* member of dimension C we get

 $\bar{y}_{ijk} = \mu + \mu_i^A + \mu_j^B + \mu_k^C + \mu_{ij}^{AB} + \mu_{jk}^{BC} + \mu_{ik}^{AC} \qquad (eq. 6)$ With the ANOVA approach we get:

- $\mu = \mu_{max}$ = overall mean of all cells of a certain aggregation level where $\mu_{i_1i_2...i_n} = y_{i_1i_2..i_n}$.
- $(\mu)_{i_p}^{A_p} = \mu_{\dots i_{p_-}} \mu$, where $\mu_{\dots i_{p_-}}$ is the mean for the p'th hierarchy in the δ_p dimension.
- $(\mu)_{i_pi_q}^{A_pA_q} = \mu_{\dots i_p\dots i_q} (\mu)_{i_p}^{A_p} (\mu)_{i_q}^{A_q} \mu$, where $\mu_{\dots i_p\dots i_q}$ is the mean for the p'th member in the δ_p dimension and the q'th member in the δ_q dimension.

The difference between the expected Value $\bar{y}_{i_1i_2...i_n}$ and the observed value $y_{i_1i_2...i_n}$ is called residual $r_{i_1i_2..i_n}$. The residuals between the actual and expected values are used to measure the significance of being exceptional. The larger the difference of the expected and the actual value is, the larger is the significance to be exceptional. Scaling problems are avoided by introducing the standardized residual $s_{i_1i_2...i_n}$ with the standard deviation $\sigma_{i_1i_2...i_n}$ as scaling factor.

as
$$s_{i_1i_2...i_n} = \left[\frac{\sigma_{i_1i_2...i_n} \sigma_{i_1i_2...i_n}}{\sigma_{i_1i_2...i_n}}\right]$$
 (eq. 7)

A cell value is exceptional if it's standardized residual is greater than a certain significance threshold value.

2. The ANOVA based log-linear model

The ANOVA based log-linear approach can be adapted to OLAP cubes. For a observed value $y_{i_1i_2...i_p}$ in a Cube G at position i_p

of the p'th dimension δ_p the expected value $\bar{y}_{i\mu_2...j_n}$ is defined as function for the various aggregation levels $g = 2^n - 1$ as:

$$\bar{y}_{i_1i_2...i_n} = \prod_{G \subset \{(\delta_1 \delta_2...\delta_n\}}^{g} \mu_{(i_p;\delta_p \in G)}^G$$
 (e.q. 8)

Which can be transformed in a linear form using the log function

$$\log(\bar{y}_{i_{1}i_{2}...i_{n}}) = \sum_{G \subset \{\delta_{1}\delta_{2}...\delta_{n}\}}^{g} \mu_{(i_{p}|\delta_{p} \in G)}^{G}$$
(eq. 8.1)

Please note that we use here the logarithm of the $\mu's$. Let us consider a cube with three dimension A, B, C. For the expected value \bar{y}_{ijk} for the *i'th* member of dimension A, the *j'th* member of dimension B and the *k'th* member of dimension C we get

 $\log(\bar{y}_{ijk}) = \mu + \mu_i^A + \mu_j^B + \mu_k^C + \mu_{ij}^{AB} + \mu_{jk}^{BC} + \mu_{ik}^{AC} \qquad (eq. 9)$ With the ANOVA approach we get:

- $\mu = \mu_{max}$ = overall mean of all cells of a certain aggregation level where $\mu_{i_1i_2..i_n} = \log(y_{i_1i_2..i_n})$
- $(\mu)_{i_p}^{A_p} = \mu_{\dots i_{p-}} \mu$, where $\mu_{\dots i_{p-}}$ is the mean for the p'th hierarchy in the δ_p dimension.
- $(\mu)_{i_p l_q}^{A_p d_q} = \mu_{\dots l_{p-l_q}} (\mu)_{l_p}^{A_p} (\mu)_{l_q}^{A_q} \mu$, where $\mu_{\dots l_{p-l_q}}$ is the mean for the p'th member in the δ_p dimension and the q'th member in the δ_q dimension.

3. Variance stabilization transformation g(x) prior to application of ANOVA method

For an observed value $y_{i_1i_2...i_n}$ in a Cube Z at position i_p of the p'th dimension δ_p the expected value $\bar{y}_{i_1i_2...i_n}$ is defined by the following function for the various aggregation levels:

$$\bar{z}_{i_1i_2\dots i_n} = \sum_{G \subset (\delta_1 \delta_2 \dots \delta_n)}^{g} \gamma^G_{(i_p; \delta_p \in G)}$$
(eq. 10)

where $\bar{z}_{i_1i_2\dots i_s}$ is a transformed value of the expected value $\bar{y}_{i_1i_2\dots i_s}$ such that $\bar{z}_{i_1i_2\dots i_s} = SIGNUM(\bar{y}_{i_1i_2\dots i_s}) * \log(|\bar{y}_{i_1i_2\dots i_s}|+1)$. (eq. 10.b) The expected value is defined as

$$\bar{y}_{i_1i_2\dots i_n} = SIGNUM(\bar{z}_{i_1i_2\dots i_n})(e^{(\bar{z}_{i_1i_2\dots i_n})} - 1).$$
(eq.11)

Let us consider a cube with three dimension A, B, C. For the expected value \bar{z}_{ijk} for the *i'th* member of dimension A, the *j'th* member of dimension B and the *k'th* member of dimension C we get

$$\bar{z}_{ijk} = \mu + \mu_i^A + \mu_j^B + \mu_k^C + \mu_{ij}^{AB} + \mu_{jk}^{BC} + \mu_{ik}^{AC} \qquad (eq. 12)$$
 With the new approach we get:

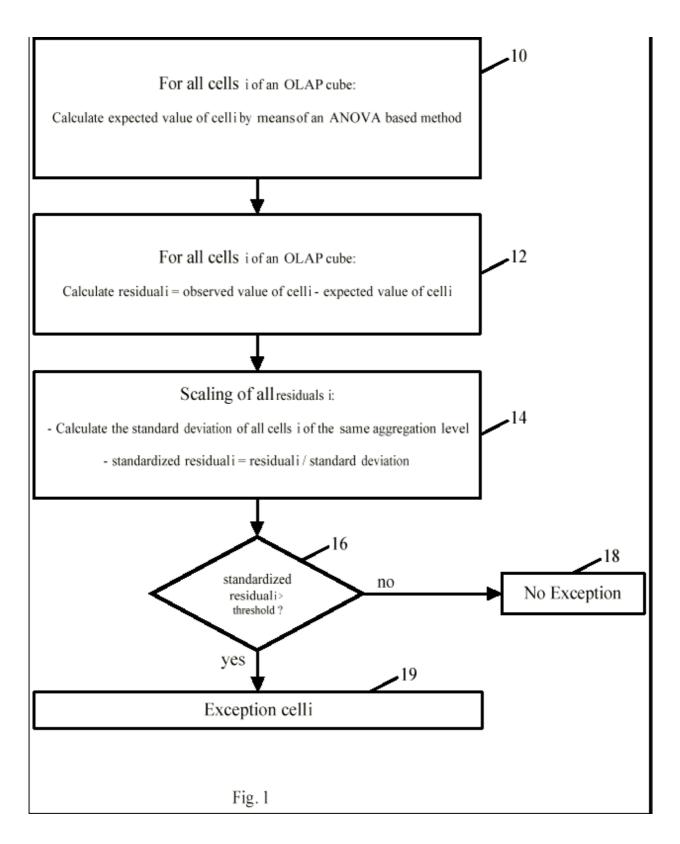
- $\mu = \mu_{\dots\dots} = \text{overall mean of all cells of a certain aggregation}$ level where $\mu_{i_1i_2\dots i_n} = z_{i_1i_2\dots i_n}$ with $z_{i_1i_2\dots i_n} = SIGNUM(y_{i_1i_2\dots i_n}) * \log y_{i_1i_2\dots i_n}|+1)$
- $(\mu)_{i_p}^{A_p} = \mu_{\dots i_{p_-}} \mu$, where $\mu_{\dots i_{p_-}}$ is the mean for the p'th hierarchy in the δ_p dimension.
- $(\mu)_{i_pi_q}^{A_pA_q} = \mu_{\dots i_{p, i_{q, \dots}}} (\mu)_{i_p}^{A_p} (\mu)_{i_q}^{A_q} \mu$, where $\mu_{\dots i_{p, i_{q, \dots}}}$ is the mean for the p'th member in the δ_p dimension and the q'th member in the δ_q dimension.

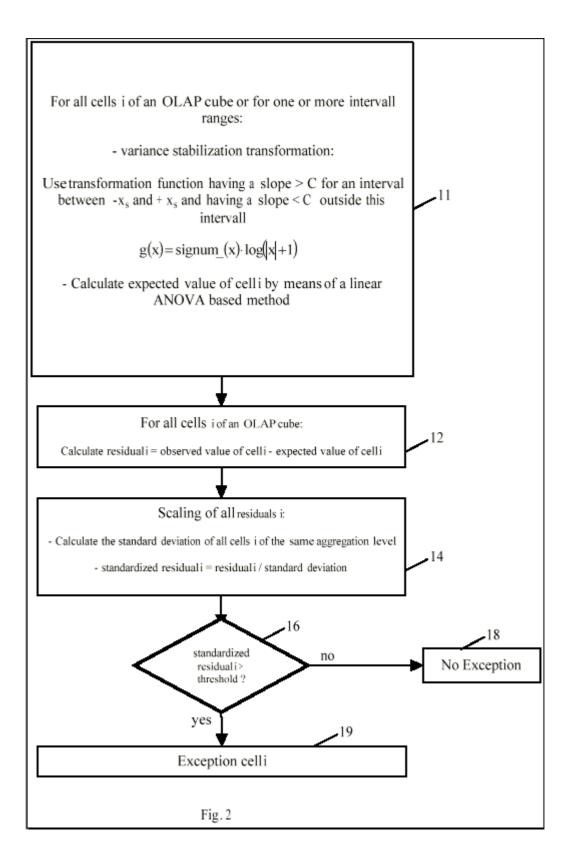
The difference between the expected Value $\bar{z}_{i_l i_2 \dots i_n}$ and the observed value $z_{i_l i_2 \dots i_n}$ is called residual $r_{i_l i_2 \dots i_n}$. The residuals between the actual and expected values are used to measure the significance for a cell to be exceptional. The standardized residual $s_{i_1 i_2 \dots i_n}$ is defined to be a multiple of the associated standard deviation $\sigma_{i_1 i_2 \dots i_n}$

$$s_{i_1i_2\dots i_n} = \left[\frac{|z_{i_1i_2\dots i_n} - \bar{z}_{i_1i_2\dots i_n}|}{\sigma_{i_1i_2\dots i_n}}\right]$$
(eq. 13)

The associated standard deviation $\sigma_{i_1i_2...i_s}$ is defined as the square root from the sum of all squared residuals which

belong to the same level of the OLAP cube where the transformed cell $z_{i_1i_2.j_n}$ exists, divided by the number of cells within this aggregation level. A cell value is exceptional if it's standardized residual is greater than a certain significance threshold value.





2 2 2 2 2 2 2 2 800 800 800 800 2 800 800 800 800 2 2 9900 2 2 2 1* Fig.3

1							
ē	Product	Business Uni	Business Unit Individual Age G Customer Ref. Customer Ant Time Period	Customer Rel	Customer Ant	Time Period	-
2	12 Month Certificate	South	Individual Age Gro, More than 15 y Annual Income FEB 1999	More than 15 y	Annual Income	FEB 1999	19
2	12 Month Certificate	South	65 And Over	More than 15 y Annual Income	Annual Income		16
Ada	Advantage Checking	North	31 to 45	Between 5 And \$20,000 to \$29	\$20,000 to \$29	MAR 1999	15
12 N	12 Month Certificate	North	31 to 45	Customer Rela Customer Anni	Customer Ann	SEP 1998	14
12 1	12 Month Certificate	Business Unit 31 to 45	31 to 45	Customer Rela, Annual Income	Amual Income	SEP 1998	14
12 M	12 Month Certificate	South	66 And Over	More than 15 y Customer Anni	Customer Ann	FEB 1999	14
12 M	12 Month Certificate	North	31 to 45	Customer Rela, Annual Income	Annual Income	SEP 1998	=
38 1	36 Month IRA Cert	Business Unit 31 to 45	31 to 45	Customer Rela Customer Anni	Customer Ann	APR 1998	ŧ
Product	uct	West	Individual Age Gro Customer Rela Annual Income	Customer Rela	Annual Income	JAN 1998	13
12 M	12 Month Certificate	North	Individual Age Gro! Customer Rela Under \$20,000	Customer Rela	Under \$20,000	FEB 1998	5
12 M	12 Month Certificate	North	31 to 45	Customer Rela, Under \$20,000	Under \$20,000	FEB 1998	13
Regu	Regular Checking	North	66 And Over	More than 15 y Annual Income JAN 1999	Annual Income	JAN 1999	13
88 M	36 Month Certificate	Business Unit	Business Unit Individual Age Gro	Customer Rela, \$40,000 to \$55	\$40,000 to \$55	AUG 1998	12
N 18	35 Month IRA Cert	Business Unit	Business Unit Individual Age Gro Customer Rela \$30,000 to \$35	Customer Rela	\$30,000 to \$35	APR 1998	12
Product	uct	North	Individual Age Gro Customer Rela Annual Income	Customer Rela	Annual income	JAN 1998	12
N IR	35 Month IRA Cert	North	31 to 45	Customer Rela Customer Ann	Customer Ann	APR 1998	12
Regu	Regular Checking	South	Individual Age Gro Customer Rela Annual Income	Customer Rela	Annual income	MAR 1999	12
12 M	12 Month Certificate	Business Unit 31 to 45	31 to 45	2 to 4 years	Customer Ann	FEB 1999	12
12 M	12 Month Certificate	Business Unit 31 to 45	31 to 45	Between 5 And Customer Ann	Customer Ann	SEP 1998	12
× 98	36 Month Certificate	Business Unit 46 to 55	46 to 55	Customer Rela, \$40,000 to \$55	\$40,000 to \$55	AUG 1998	12
12 M	12 Month Certificate	Business Unit 31 to 45	31 to 45	Customer Rela Under \$20 000	Under \$20 000	FEB 1998	12
12 M	12 Month Certificate	Business Unit	Individual Age Gro	Between 5 And Under \$20,000	Under \$20,000	FEB 1996	12
6 Ma	6 Month Certificate	North	31 to 45	Customer Rela, Under \$20,000	Under \$20,000	FEB 1998	12
Regu	Regular Checking	North	Individual Age Gro	Between 5 And \$30,000 to \$35	\$30,000 to \$35	MAR 1999	12
Regu	Regular Checking	North	Individual Age Gro. Between 5 And Under \$20,000	Between 5 And	Under \$20,000	-	12
1 C M	12 Month Certificate	Business Unit 31 to 45	31 to 45	Between 5 And Annual Income	Annual Income	SFP 1998	12

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	 Years North South East West 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	
	l Years North South East West	
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DUSINEES UNIT	Geogr	aphy					
Customer Rela	dionshi	ip Age					
\$60,000 to \$79,999	666					-	and the second se
Profit							
		JAN 1999	FEB 1999	JAN 1999 FEB 1999 MAR 1999 APR 1999	PR 1999		
Less Than 18							
19 to 30		0	0	0	0		and the second se
31 to 45		57.41	7.46	56.14	8		
46 to 55		1.31	2.8	-0.87	-		
56 to 64							
65 And Over		14.72	-1.86	46.23	0		
	-						
							 No. of Concession, Name

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	P 5	October	November	December
12	Product A	993	887	927
	Product B	801	756	847
	Product C		9	-54
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Fig.7

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1. A method for determination of an exception in multidimensional data, the method comprising the steps of:

- e) determination of an expected value for a set of cells of the multi-dimensional data by means of an ANOVA based method,
- f) determination of a residual for each cell of the set of cells,
- g) scaling of the residuals,
- h) comparing the scaled residuals with a threshold value for determination of the exception.
- 2. The method of claim 1 the multi-dimensional data being stored in an OLAP data base.
- 3. The method of claim 1 or 2 further comprising the step of performing a variance stabilization transformation prior to the step of determining of an expected value.
- The method of claims 1, 2 or 3 the variance stabilization transformation comprising a non-linear transformation function.
- 5. The method of claim 3 or 4 the variance stabilization transformation comprising reducing the weight of large absolute data values with respect to low absolute data values of the multi-dimensional data.

- 6. The method of claims 3, 4 or 5, the variance stabilization transformation comprising a transformation function having a slope greater than a constant for a data interval comprising 0 and having a slope lesser than the constant outside the data interval.
- 7. The method of anyone of the preceding claims 3 to 6 the variance stabilization transformation being performed with respect to all data values or a selected sub-set of data values.
- 8. The method of anyone of the preceding claims 1 to 7 the ANOVA based method being a linear ANOVA based method.
- 9. The method of anyone of the preceding claims 1 to 8 the residual being calculated by subtracting the expected value from the observed value of the corresponding cell.
- 10. The method of anyone of the preceding claims 1 to 9, the scaling of the residuals comprising calculating the standard deviation of the residuals from all cells of the same aggregation level and standardizing the residual of that aggregation level by dividing the residual by the associated standard deviation.
- 11. The method of anyone of the preceding claims 1 to 10, whereby the exception is determined within the same aggregation level.
- 12. The method of claim 11, whereby the aggregation level is user specified.
- 13. A computer program product stored on a computer usable medium comprising computer readable program means for causing a computer system to perform a method according to

anyone of the preceding claims 1 to 11 when the program is run on the computer system.

- 14. A data processing program for execution on a computer system for performing a method according to anyone of the preceding claims 1 to 12 when the data processing program is run on the computer system.
- 15. A computer system comprising means adapted for carrying out the steps of anyone of the preceding claims 1 to 12.